



#### **Mathematics**

#### 5th Grade

#### Standard 1 - Number Sense

Students compute with whole numbers\*, decimals, and fractions and understand the relationship among decimals, fractions, and percents. They understand the relative magnitudes of numbers. They understand Prime\* and composite\* numbers.

5.1.1 Convert between numbers in words and numbers in figures, for numbers up to millions and decimals to thousandths.

Example: Write the number 198,536 in words.

5.1.2 Round whole numbers and decimals to any place value.

Example: Is 7,683,559 closer to 7,600,000 or 7,700,000? Explain your answer.

5.1.3 Arrange in numerical order and compare whole numbers or decimals to two decimal places by using the symbols for less than (<), equals (=), and greater than (>).

Example: Write from smallest to largest: 0.5, 0.26, 0.08.

5.1.4 Interpret percents as a part of a hundred. Find decimal and percent equivalents for common fractions and explain why they represent the same value.

Example: Shade a 100-square grid to show 30%. What fraction is this?

5.1.5 Explain different interpretations of fractions: as parts of a whole, parts of a set, and division of whole numbers by whole numbers.

Example: What fraction of a pizza will each person get when 3 pizzas are divided equally among 5 people?

5.1.6 Describe and identify prime and composite numbers.

Example: Which of the following numbers are prime: 3, 7, 12, 17, 18? Justify your choices.

5.1.7 Identify on a number line the relative position of simple positive fractions, positive mixed numbers, and positive decimals.

Example: Find the positions on a number line of 11/4 and 1.4.

<sup>\*</sup>whole numbers: 0, 1, 2, 3, etc.

<sup>\*</sup>prime number: number that can be evenly divided only by 1 and itself (e.g., 2, 3, 5, 7, 11)

<sup>\*</sup>composite number: not a prime number (e.g., 4, 6, 8, 9, 10)





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### Standard 2 - Computation

Students solve problems involving multiplication and division of whole numbers and solve problems involving addition, subtraction, and simple multiplication and division of fractions and decimals.

5.2.1 Solve problems involving multiplication and division of any whole numbers.

Example:  $2,867 \times 34 = ?$  Explain your answer.

5.2.2 Add and subtract fractions (including mixed numbers) with different denominators.

Example:  $3\frac{4}{5} - 2\frac{2}{3} = ?$ 

5.2.3 Use models to show an understanding of multiplication and division of fractions.

Example: Draw a rectangle 5 squares long and 3 squares wide. Shade  $\frac{4}{5}$  of the rectangle, starting from the left. Shade  $\frac{2}{3}$  of the rectangle, starting from the top. Look at the fraction of the squares that you have double-shaded and use that to show how to multiply  $\frac{4}{5}$  by  $\frac{2}{3}$ .

5.2.4 Multiply and divide fractions to solve problems.

Example: You have  $3\frac{1}{2}$  pizzas left over from a party. How many people can have  $\frac{1}{4}$  of a pizza each?

5.2.5 Add and subtract decimals and verify the reasonableness of the results.

Example: Compute 39.46 – 20.89 and check the answer by estimating.

5.2.6 Use estimation to decide whether answers are reasonable in addition, subtraction, multiplication, and division problems.

Example: Your friend says that  $2,867 \times 34 = 20,069$ . Without solving, explain why you think the answer is wrong.

5.2.7 Use mental arithmetic to add or subtract simple decimals.

Example: Add 0.006 to .027 without using pencil and paper.





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#### Standard 3 – Algebra and Functions

Students use variables in simple expressions, compute the value of an expression for specific values of the variable, and plot and interpret the results. They use two-dimensional coordinate grids to represent points and graph lines.

5.3.1 Use a variable to represent an unknown number.

Example: When a certain number is multiplied by 3 and then 5 is added, the result is 29. Let x stand for the unknown number and write an equation for the relationship.

5.3.2 Write simple algebraic expressions in one or two variables and evaluate them by substitution.

Example: Find the value of 5x + 2 when x = 3.

5.3.3 Use the distributive property\* in numerical equations and expressions.

Example: Rewrite 3(16-11) by removing the parentheses.

5.3.4 Identify and graph ordered pairs of positive numbers.

Example: Plot the points (3, 1), (6, 2), and (9, 3). What do you notice?

5.3.5 Find ordered pairs (positive numbers only) that fit a linear equation, graph the ordered pairs, and draw the line they determine.

Example: For x = 1, 2, 3, and 4, find points that fit the equation y = 2x + 1. Plot those points on graph paper and join them with a straight line.

5.3.6 Understand that the length of a horizontal line segment on a coordinate plane equals the difference between the *x*-coordinates and that the length of a vertical line segment on a coordinate plane equals the difference between the *y*-coordinates.

Example: Find the distance between the points (2, 5) and (7, 5) and the distance between the points (2, 1) and (2, 5).

5.3.7 Use information taken from a graph or equation to answer questions about a problem situation.

Example: The speed (v feet per second) of a car t seconds after it starts is given by the formula v = 12t. Find the car's speed after 5 seconds.

\*distributive property: e.g.,  $3 \times (5 \div 2) = 3 \times 5 \times 3 \times 2$ 





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#### Standard 4 – Geometry

Students identify, describe, and classify the properties of plane and solid geometric shapes and the relationships between them.

- 5.4.1 Measure, identify, and draw angles, perpendicular and parallel lines, rectangles, triangles, and circles by using appropriate tools (e.g., ruler, compass, protractor, appropriate technology, media tools).

  Example: Draw a rectangle with sides 5 in and 3 in.
- 5.4.2 Identify, describe, draw, and classify triangles as equilateral\*, isosceles\*, scalene\*, right\*, acute\*, obtuse\*, and equiangular\*.
  - Example: Draw an isosceles right triangle.
- 5.4.3 Identify congruent\* triangles and justify your decisions by referring to sides and angles.
  - Example: In a collection of triangles, pick out those that are the same shape and size and explain your answers.
- 5.4.4 Identify, describe, draw, and classify polygons\*, such as pentagons and hexagons.
  - Example: In a collection of polygons, pick out those with the same number of sides.
- 5.4.5 Identify and draw the radius and diameter of a circle and understand the relationship between the radius and diameter.
  - Example: On a circle, draw a radius and a diameter and describe the differences and similarities between the two.
- 5.4.6 Identify shapes that have reflectional and rotational symmetry\*.
  - Example: What kinds of symmetries have the letters M, N, and O?
- 5.4.7 Understand that 90°, 180°, 270°, and 360° are associated with 1/4, 1/2, 3/4, and full turns, respectively.
  - Example: Face the front of the room. Turn through four right angles. Which way are you now facing?
- 5.4.8 Construct prisms\* and pyramids using appropriate materials.
  - Example: Make a square-based pyramid from construction paper.
- 5.4.9 Given a picture of a three-dimensional object, build the object with blocks.

Example: Given a picture of a house made of cubes and rectangular prisms, build the house.

- \*equilateral triangle: all sides are congruent
- \*isosceles triangle: at least two sides are congruent
- \*scalene triangle: no sides are equal
- \*right triangle: one angle measures 90 degrees
- \*acute triangle: all angles are less than 90 degrees
- \*obtuse triangle: one angle is more than 90 degrees
- \*equiangular triangle: all angles are of equal measure
- \*congruent: two figures that are the same shape and size
- \*polygon: two-dimensional shape with straight sides (e.g., triangle, rectangle, pentagon)
- \*reflectional and rotational symmetry: letter M has reflectional symmetry in a line down the middle; letter N has rotational symmetry around its center
- \*prism: solid shape with fixed cross-section (right prism is a solid shape with two parallel faces that are polygons and other faces that are rectangles)







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#### Standard 5 – Measurement

Students understand and compute the areas and volumes of simple objects, as well as measuring weight, temperature, time, and money.

- 5.5.1 Understand and apply the formulas for the area of a triangle, parallelogram, and trapezoid.
  - Example: Find the area of a triangle with base 4 m and height 5 m.
- 5.5.2 Solve problems involving perimeters and areas of rectangles, triangles, parallelograms, and trapezoids, using appropriate units.
  - Example: A trapezoidal garden bed has parallel sides of lengths 14 m and 11 m and its width is 6 m. Find its area and the length of fencing needed to enclose it. Be sure to use correct units.
- 5.5.3 Use formulas for the areas of rectangles and triangles to find the area of complex shapes by dividing them into basic shapes.
  - Example: A square room of length 17 feet has a tiled fireplace area that is 6 feet long and 4 feet wide. You want to carpet the floor of the room, except the fireplace area. Find the area to be carpeted.
- 5.5.4 Find the surface area and volume of rectangular solids using appropriate units.
  - Example: Find the volume of a shoe box with length 30 cm, width 15 cm, and height 10 cm.
- 5.5.5 Understand and use the smaller and larger units for measuring weight (ounce, gram, and ton) and their relationship to pounds and kilograms.
  - Example: How many ounces are in a pound?
- 5.5.6 Compare temperatures in Celsius and Fahrenheit, knowing that the freezing point of water is 0°C and 32°F and that the boiling point is 100°C and 212°F.
  - Example: What is the Fahrenheit equivalent of 50°C? Explain your answer.
- 5.5.7 Add and subtract with money in decimal notation.
  - Example: You buy articles that cost \$3.45, \$6.99, and \$7.95. How much change will you receive from \$20?





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#### Standard 6 – Data Analysis and Probability

Students collect, display, analyze, compare, and interpret data sets. They use the results of probability experiments to predict future events.

- 5.6.1 Explain which types of displays are appropriate for various sets of data.
  - Example: Conduct a survey to find the favorite movies of the students in your class. Decide whether to use a bar, line, or picture graph to display the data. Explain your answer.
- 5.6.2 Find the mean\*, median\*, mode\*, and range\* of a set of data and describe what each does, and does not, tell about the data set.
  - Example: Find the mean, median, and mode of a set of test results and describe how well each represents the data.
- 5.6.3 Understand that probability can take any value between 0 and 1, events that are not going to occur have probability 0, events certain to occur have probability 1, and more likely events have a high probability than less likely events.
  - Example: What is the probability of rolling a 7 with a number cube?
- 5.6.4 Express outcomes of experimental probability situations verbally and numerically (e.g., 3 out of 4, 3/4).
  - Example: What is the probability of rolling an odd number with a number cube?

<sup>\*</sup>mean: the average obtained by adding the values of and dividing by the number of values \*median: the value that divides a set of data written in order of size into two equal parts

<sup>\*</sup>mode: the most common value in a set of data

<sup>\*</sup>range: the difference between the largest and smallest number





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#### Standard 7 - Problem solving

Students make decisions about how to approach problems and communicate their ideas.

- 5.7.1 Analyze problems by identifying relationships, telling relevant from irrelevant information, sequencing and prioritizing information, and observing patterns.
  - Example: Solve the problem: "When you flip a coin 3 times, you can get 3 heads, 3 tails, 2 heads, and 1 tail, or 1 head and 2 tails. Find the probability of each of these combinations." Notice that the case of 3 heads and the case of 3 tails are similar. Notice that the case of 2 heads and 1 tail and the case of 1 head and 2 tails are similar.
- 5.7.2 Decide when and how to break a problem into simpler parts.
  - Example: In the first example, decide to look at the case of 3 heads and the case of 2 heads and 1 tail.

Students use strategies, skills, and concepts in finding and communicating solutions to problems.

- 5.7.3 Apply strategies and results from simpler problems to solve more complex problems.
  - Example: In the first example, begin with the situation where you flip the coin twice.
- 5.7.4 Express solutions clearly and logically by using the appropriate mathematical terms and notation. Support solutions with evidence in both verbal and symbolic work.
  - Example: In the first example, make a table or tree diagram to show another student what is happening.
- 5.7.5 Recognize the relative advantages of exact and approximate solutions to problems and give answers to a specified degree of accuracy.
  - Example: You are buying a piece of plastic to cover the floor of your bedroom before you paint the room. How accurate should you be: to the nearest inch, foot, or yard? Explain your answer.
- 5.7.6 Know and apply appropriate methods for estimating results of rational-number computations.
  - Example: Will 7 x 18 be smaller or larger than 100? Explain your answer.
- 5.7.7 Make precise calculations and check the validity of the results in the context of the problem.
  - Example: A recipe calls for  $\frac{3}{8}$  of a cup of sugar. You plan to double the recipe for a party and you have only one cup of sugar in the house. Decide whether you have enough sugar and explain how you know.

Students determine when a solution is complete and reasonable and move beyond a particular problem by generalizing to other situations.

- 5.7.8 Decide whether a solution is reasonable in the context of the original situation.
  - Example: In the first example about flipping a coin, check that your probabilities add to 1.
- 5.7.9 Note the method of finding the solution and show a conceptual understanding of the method by solving similar problems.
  - Example: Find the probability of each of the combinations when you flip a coin 4 times.